

1.5 Trigonometrijske funkcije

1. Izračunati vrednost ostalih trigonometrijskih funkcija ako je:

$$(a) \quad \cos \alpha = \frac{12}{13}, \quad 0 < \alpha < \frac{\pi}{2},$$

$$(b) \quad \sin \alpha = \frac{3}{5}, \quad \frac{\pi}{2} < \alpha < \pi,$$

$$(c) \quad \sin \alpha = -\frac{2}{\sqrt{13}}, \quad \pi < \alpha < \frac{3\pi}{2}.$$

2. Izračunati $\sin(\alpha - \beta)$ ako je $\sin \alpha = \frac{\sqrt{2}}{2}$, $\cos \beta = \frac{3}{5}$, $0 < \alpha, \beta < \frac{\pi}{2}$.

3. Izračunati $\cos(\alpha + \beta)$ ako je $\cos \alpha = -\frac{\sqrt{2}}{2}$, $\sin \beta = \frac{3}{5}$, $\frac{\pi}{2} < \alpha < \pi$, $0 < \beta < \frac{\pi}{2}$.

4. Izračunati $\sin 2\alpha$ ako je $\sin \alpha = -\frac{4}{5}$, $\pi < \alpha < \frac{3\pi}{2}$.

5. Izračunati $\cot 2\alpha$ ako je $\cos \alpha = \frac{12}{13}$, $\frac{3\pi}{2} < \alpha < 2\pi$.

Rešenja

$$1. \quad (a) \quad \sin \alpha = \frac{5}{13}, \quad \tan \alpha = \frac{5}{12}, \quad \cot \alpha = \frac{12}{5},$$

$$(b) \quad \cos \alpha = -\frac{4}{5}, \quad \tan \alpha = -\frac{3}{4}, \quad \cot \alpha = -\frac{4}{3},$$

$$(c) \quad \cos \alpha = -\frac{3}{\sqrt{13}}, \quad \tan \alpha = \frac{2}{3}, \quad \cot \alpha = \frac{3}{2}$$

$$2. \quad \sin(\alpha - \beta) = -\frac{\sqrt{2}}{10} \quad (\cos \alpha = \frac{\sqrt{2}}{2}, \sin \beta = \frac{4}{5})$$

$$3. \quad \cos(\alpha + \beta) = -\frac{7\sqrt{2}}{10} \quad (\sin \alpha = \frac{\sqrt{2}}{2}, \cos \beta = \frac{4}{5})$$

$$4. \quad \sin 2\alpha = -\frac{7}{25} \quad (\cos \alpha = -\frac{3}{5})$$

$$5. \quad \cot 2\alpha = -\frac{119}{120} \quad (\sin \alpha = -\frac{5}{13}, \cot \alpha = -\frac{12}{5})$$